# Students Enrolled in Probability and Statistics for the 2020-2021 School Year Summer Packet

#### Name:

This packet is to help you review various topics that are considered to be prerequisite knowledge upon entering Probability and Statistics. In order to ensure that the good skills you developed in previous math courses do not disappear, working on this packet is highly recommended over the summer. A good habit would be to do at least one math problem every day. Enjoy your summer, but be sure to come prepared with the necessary knowledge to continue into Probability and Statistics next year. These skills and topics will be assessed in the fall.

Frequency Tables, Line Plots, and Histograms

# Aimee asked students in her grade

how many CDs they own. She displayed her data in a frequency table. Each tally stands for 1 CD.

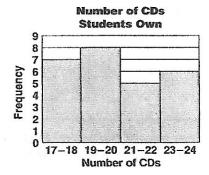
#### Students' CD Collections

| Number of CDs | 17  | 18 | 19   | 20 | 21 | 22   | 23 | 24   |
|---------------|-----|----|------|----|----|------|----|------|
| Tally         | 441 | ı  | 1111 | Ш  | ı  | 1111 | 11 | 1111 |
| Frequency     | 6   | 1  | 5    | 3  | 1  | 4    | 2  | 4    |

She displayed the same data in a line plot. Each X stands for 1 CD.

|        | ımbe | er of | CDs | Stu | dent | s Ow | 'n |
|--------|------|-------|-----|-----|------|------|----|
| X<br>X |      | х     |     |     |      |      |    |
| X      |      | X     |     |     | Х    |      | Х  |
| X      |      | X     | X   |     | X    |      | X  |
| X      |      | X     | X   |     | X    | X    | X  |
| X      | Х    | X     | Х   | X   | Х    | X    | X  |
| 17     | 18   | 19    | 20  | 21  | 22   | 23   | 24 |

She also made a histogram to show the frequencies. The bars represent intervals of equal size. The height of each bar gives the frequency of the data.



#### Use the frequency table for Exercises 1-3.

- 1. Ms. Ortiz's class is planning a school garden. She asked her students how many rose bushes they want in the garden. She recorded the data in a frequency table. Complete the table.
- 2. Use the frequency table to make a line plot for the data.
- 3. Draw a histogram of the students' data.

| Number of<br>Rose Bushes | 1 | 2    | 3   | 4     | 5    | 6    |
|--------------------------|---|------|-----|-------|------|------|
| Tally                    | ı | 1111 | 111 | 11111 | 1    | ı. I |
| Frequency                |   |      |     | F     | 1111 |      |

# **Circle Graphs**

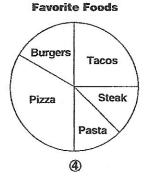
The class took a survey of favorite foods.

The results are shown in the table and the circle graph.

To make a circle graph:

- 1 Find the total number of votes.
- ② Find each part of the total as a fraction or percent.
- 3 Find the measure of each central angle in the circle graph.
- Draw, label, and title the graph.

| Food    | Votes    | ②<br>Fraction              | %                  | ③<br>Degrees |
|---------|----------|----------------------------|--------------------|--------------|
| Burgers | 8        | $\frac{8}{48}=\frac{1}{6}$ | $16\frac{2}{3}\%$  | 60°          |
| Pizza   | 16       | 1/3                        | 33 <del>1</del> 3% | 120°         |
| Steak   | 6        | 1/8                        | 121/2%             | 45°          |
| Tacos   | 12       | 1/4                        | 25%                | 90°          |
| Pasta   | 6        | 1/8                        | 121/2%             | 45°          |
| Total   | <b>1</b> |                            |                    | 360°         |



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Find the measure of the central angle that represents each fraction or percent in a circle graph.

**1.** 
$$\frac{1}{5}$$
 **2.** 40% **3.**  $\frac{1}{2}$  **4.** 5% **4.** 5%

**Monthly Family** Budget

Item

Rent

Food

Gas

Phone

Misc.

Clothes

6. 
$$\frac{1}{10}$$
 \_\_\_\_\_

**5.** 35% \_\_\_\_\_ **6.** 
$$\frac{1}{10}$$
 \_\_\_\_\_ **7.** 20% \_\_\_\_\_ **8.**  $\frac{1}{12}$  \_\_\_\_\_

Display the data in each table in a circle graph.

9. a monthly family budget

Amount

\$425

\$150

\$50

\$75

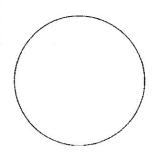
\$25

\$100

|  | \ |
|--|---|
|  |   |

10. number of children per family

| Children per<br>Family |          |  |  |  |
|------------------------|----------|--|--|--|
| Children               | Families |  |  |  |
| 0                      | 4        |  |  |  |
| 1                      | 15       |  |  |  |
| 2                      | 20       |  |  |  |
| 3                      | 13       |  |  |  |
| 4                      | 5        |  |  |  |
| 5                      | 3        |  |  |  |



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## Stem-and-Leaf Plots

A stem-and-leaf plot is an easy way to show data arranged in order.

8th Grade 100-M Dash (Times to Nearest 0.1 s)

| 13.1 | 16.2 | 15.5 | 15.2 | 13.5 |
|------|------|------|------|------|
| 15.3 | 14.8 | 14.4 | 17.5 | 12.2 |
| 14.1 | 16.1 | 16.9 | 15.3 | 16.8 |
| 16.0 | 15.3 | 12.0 | 18.2 | 14.6 |
| 13.2 | 18.3 | 16.6 | 15.3 | 18.8 |

① Choose stems. The times range from 12.0 to 18.8. Choose 12 to 18 as stems.

2 List the tenths digits as leaves.

| 18 | 238    |
|----|--------|
| 17 | 5      |
| 16 | 012689 |
| 15 | 233335 |
| 14 | 1468   |
| 13 | 125    |
| 12 | 02     |

3 Make a key to explain what each stem and leaf represents.

18 | 2 means 18.2

The mode is the most frequent number.

The mode is 15.3 seconds.

The range is the greatest number minus the least number.

The range is 18.8 - 12.0 = 6.8 seconds.

The **median** is the middle number or average of the middle two numbers. The median is 15.3 seconds.

1. Complete the stem-and-leaf plot for the data.

#### 8th Grade 200-M Dash (Times to Nearest 0.1 s)

| 32.1 | 38.5                 | 31.7                                | 34.7   |
|------|----------------------|-------------------------------------|--|
| 35.2 | 34.4                 | 30.2                                | 35.3   |
| 31.9 | 36.0                 | 32.2                                | 36.7   |
| 31.4 | 34.7                 | 29.5                                | 36.9   |
| 33.4 | 38.6                 | 34.7                                | 37.3   |
|      | 35.2<br>31.9<br>31.4 | 35.2 34.4<br>31.9 36.0<br>31.4 34.7 | 35.2 34.4 30.2<br>31.9 36.0 32.2<br>31.4 34.7 29.5 |

#### Times for the 200-M Dash

| 38 |  |
|----|--|
| 37 |  |
| 36 |  |
| 35 |  |
| 34 |  |
| 33 |  |
| 32 |  |
| 31 |  |
| 30 |  |
| 29 |  |

Use your stem-and-leaf plot for Exercises 2-5.

- 2. The mode is \_\_\_\_\_.
- 3. The range is \_\_\_\_\_.
- 4. The median is
- 5. How many 8th grade students finished the race in less than 35 s?

Percent of Federally Owned Land in Ten Western States

45% 24% 52% 61% 28%

42% 34% 48% 63% 36%

## **Box-and-Whisker Plots**

#### Make a box-and-whisker plot for the data set.

Step 1: First list the data in order from least to greatest. Find the median.

24 28 34 36 42 | 45 48 52 61 63

Since there is an even number of percents (10),

there are two middle numbers. Add them and divide by 2.

$$\frac{42+45}{2} = \frac{87}{2} = 43.5$$

The median is 43.5.

Step 2: Find the upper and lower quartiles.

The lower quartile is the median of the lower half.

24 28 34 36 42

The lower quartile is 34.

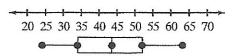
The upper quartile is the median of the upper half.

45 48 52 61 63

The upper quartile is 52.

Step 3: Draw a number line. Mark the least and greatest values, the median, and the quartiles. Draw a box from the first to the third quartiles. Draw whiskers from the least and greatest values to the box.

The data range from 24 to 63. A scale of 5 from 20 to 70 would have



### Make a box-and-whisker plot for each data set.

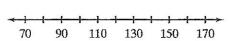
1. area in 1,000 mi<sup>2</sup> of 13 western states

122 164 71 98 84 147 114 111 98 85 104 71 77

median:

lower quartile:

upper quartile:



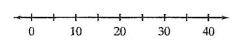
2. percent of area that is inland water for 11 northeastern states

13% 4% 26% 4% 32% 13% 15% 3% 21% 7% 21%

median:

lower quartile:

upper quartile:



## **Scatter Plots and Trends**

Gilbert is investigating the relationship between the number of credit cards a person has and the amount of credit card debt.

First, he made a table of his data.

Credit Cards and Credit Card Debt

| Number of Cards | Amount of Debt |
|-----------------|----------------|
| 1               | \$0            |
| 1               | \$1,000        |
| 1               | \$5,000        |
| 2               | \$3,000        |
| 2               | \$5,000        |
| 3               | \$10,000       |
| 3               | \$5,000        |
| 3               | \$8,000        |
| 4               | \$10,000       |
| 5               | \$19,000       |

Then he plotted the data in a scatter plot.



Gilbert's scatter plot shows a positive trend in the data. That means as the number of credit cards goes up so does the amount of debt. As one value goes up, so does the other.

In a negative trend, one value goes up while the other goes down.

1. Dana surveyed her friends about how much TV they watch and their average test scores. Her results are shown below. Complete the scatter plot for the data.

Test Scores and TV

| TV Hours<br>Per Day | Average<br>Test Score | TV Hours<br>Per Day | Average<br>Test Score |  |  |  |  |
|---------------------|-----------------------|---------------------|-----------------------|--|--|--|--|
| 1                   | 98                    | 3                   | 79                    |  |  |  |  |
| 1                   | 86                    | 3                   | 73                    |  |  |  |  |
| 2                   | 90                    | 3                   | 75                    |  |  |  |  |
| 2                   | 82                    | 4                   | 62                    |  |  |  |  |
| 2                   | 85                    | 5                   | 68                    |  |  |  |  |
|                     |                       |                     |                       |  |  |  |  |

**Test Scores and TV** 100 **Test Scores** 80

70 60



- 2. Is the trend in the data negative or positive? Explain.
- 3. Describe the relationship Dana likely found between test scores and TV time.
- 26 Data Analysis and Probability Workbook

26

26

Number of Pages Read by Members of the Science Fiction Book Club

27

26

26

23

27

29

## **Measures of Central Tendency**

The median of this set of data is the middle value when the scores are ordered.

23 25 25 26 26 26 26 26 27 27 28 29

Since there are two middle scores, add them and divide by 2.

$$\frac{26+26}{2}=26$$

The mean is the sum of the scores divided by the number of scores.

$$25 + 26 + 28 + 25 + 26 + 27 + 27 + 26 + 26 + 29 + 26 + 23 = 314$$

$$\frac{314}{12}$$
 = 26.166667, or about 26.2 pages

The mode is the score that occurs the most. The mode is 26 pages.

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Choose a calculator, pencil and paper, or mental math. Find the mean, median, and mode of each set of data.

- 1. movies seen: 3 3 1 4 0 4 2 5 7 4 1 2
- 2. miles hiked: 5 10 9 12 8 4 5 7 5 13 11
- 3. runs scored: 0 0 8 4 15 9 1 1 6 7 10 2
- 4. costs of a ride:

\$3.25 \$2.50 \$4.00 \$4.00 \$3.50 \$2.00 \$4.00 \$3.00 \$2.50 \$3.00 \$4.00

Name the measure of central tendency you would report to your parents. Give your reason.

5. test scores: 89 84 79 80 81 55

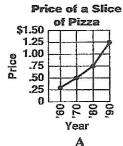
6. friends' allowances: \$10 \$15 \$12 \$15 \$8

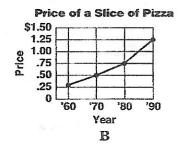
# Misleading Graphs

Data can be displayed on graphs in ways that are misleading.

The horizontal scales make these graphs seem different.

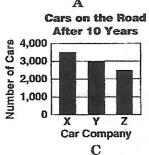
As the numbers are moved farther apart, it appears that the change over time is less.

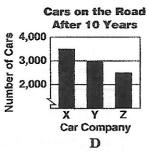




These graphs may seem different because of how the vertical scales are drawn.

The break in the vertical scale makes the differences seem greater than they really are.





Use the graphs above to answer Exercises 1-6.

- 1. Which graph might be used to convince someone that the price of pizza has risen too quickly over the years?
- 2. Which graph might be used to convince someone that pizza makers should raise their prices?
- 3. Name 2 ways in which the pizza graphs differ.
- **4.** Which graph would Car Company X use to show that its cars last longer than the competition?
- 5. Which graph of cars still on the road after 10 years would Car Company Z prefer?
- 6. Name 2 ways in which graphs C and D differ.

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### Example

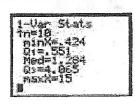
Enter the data from the table at the right. Find the mean, median, standard deviation, and the first and third quartiles.

STEP 1: Enter the tourist data into list L1 by pressing

| ILZ      | 12.3 | İ     |
|----------|------|-------|
| 1        | ·    |       |
| i        | F    |       |
| 1        |      |       |
|          | ŧ    |       |
| <u> </u> |      |       |
|          | 12   | 12 23 |

STEP 2: View the statistics for the tourists visiting the United States by pressing STAT 1 ENISE. Press Trive times to scroll to the bottom of the statistics.





The 10 Most America-Loving Countries

| Country     | Tourists (in millions) |  |  |  |  |
|-------------|------------------------|--|--|--|--|
| Canada      | 15.0                   |  |  |  |  |
| Mexico      | 11.325                 |  |  |  |  |
| Japan       | 4.065                  |  |  |  |  |
| Britain     | 2.921                  |  |  |  |  |
| Germany     | 1.705                  |  |  |  |  |
| France      | 0.863                  |  |  |  |  |
| Brazil      | 0.661                  |  |  |  |  |
| Italy       | 0.551                  |  |  |  |  |
| South Korea | 0.504                  |  |  |  |  |
| Venezuela   | 0.424                  |  |  |  |  |

Source: Time Magazine

Note: By default the TI-83/TI-83 Plus looks for data in L1. If the data is stored elsewhere, the list name must follow 'L-VAR Stats'.

Q3:

STATISTICS: The following table identifies the statistical symbols.

x: mean of entries

Sx: sample standard deviation

Q1: first quartile of entries

Σx: sum of entries

ox: population standard deviation

Med: median of entries

 $\Sigma x^2$  sum of the squares of entries

total number of entries

third quartile of entries

\*

minX: smallest entry

maxX: largest entry

## Exercises

Enter the data. Find the mean, median, standard deviation, and the first and third quartiles.

1

#### State Gasoline Taxes in 1992 (¢/gal)

| State | AK | AR   | СО | DE | FL   | Ш  | IL | IA | KY | ME | MA | MN |
|-------|----|------|----|----|------|----|----|----|----|----|----|----|
| Tax   | 8  | 18.5 | 22 | 19 | 4    | 16 | 19 | 20 | 15 | 19 | 21 | 20 |
| State | МО | NE   | NH | NM | NC   | ОН | OR | RI | SD | TX | VT | WA |
| Tax   | 13 | 23.7 | 18 | 16 | 22.3 | 21 | 22 | 23 | 18 | 20 | 15 | 23 |

Source: The Universal Almanac 1996